



Using Regression-based Sensitivity Analysis in Exploratory Modeling of Complex Spatial Systems: An Example of Simulating the Impact of Agricultural Water Withdrawals on Fish Habitat

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Research Question:

What issues arise in employing regression techniques to evaluate the sensitivity of a complex, agent-based spatial model to its individual parameters?

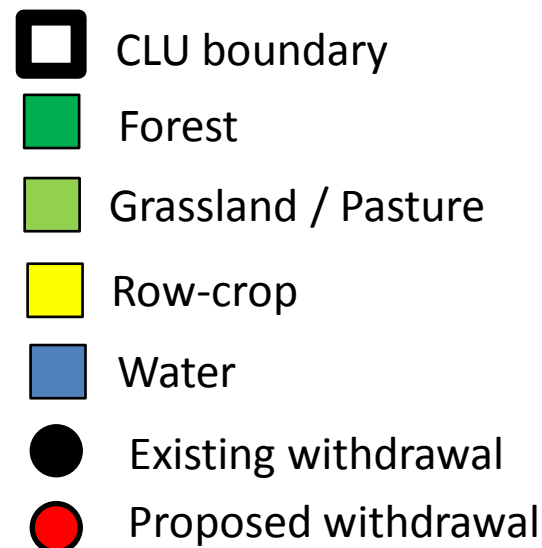
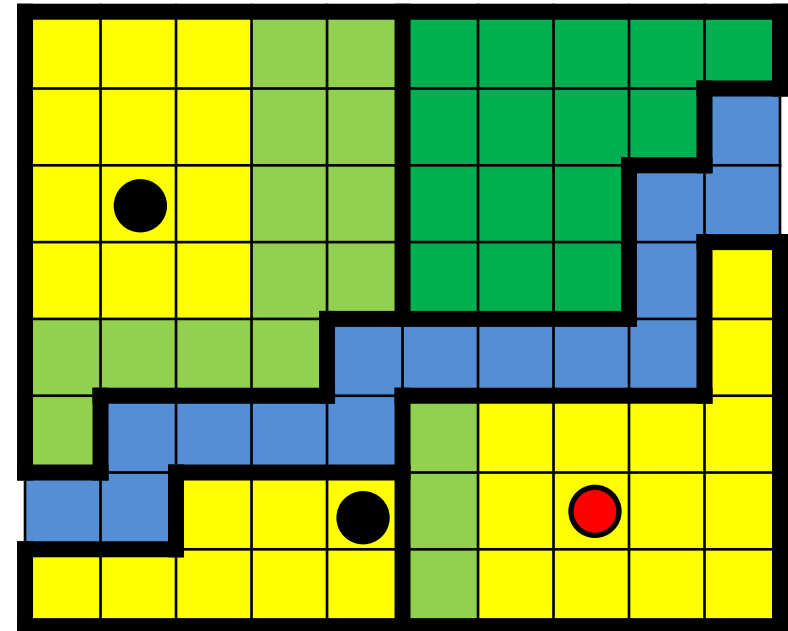
Overview:

- Conceptual agent-based model of fish habitat impacts from agricultural water withdrawals.
- Model sensitivity analysis through OLS regression.
- Issues with count data
- OLS alternative: negative binomial with hurdle

Conceptual Model

- Farmlands (CLUs)
(land owner agents)
- Agricultural Demand Index
- Likelihood of CRP enrollment
- Land use change decisions –
withdrawal installations
- **Reductions in baseflow¹**
- **Decline in fish sustainability²**

1. Reeves 2008.
2. Zorn, et. al. 2008.



Regression-based Sensitivity

Introduction

ABM Model

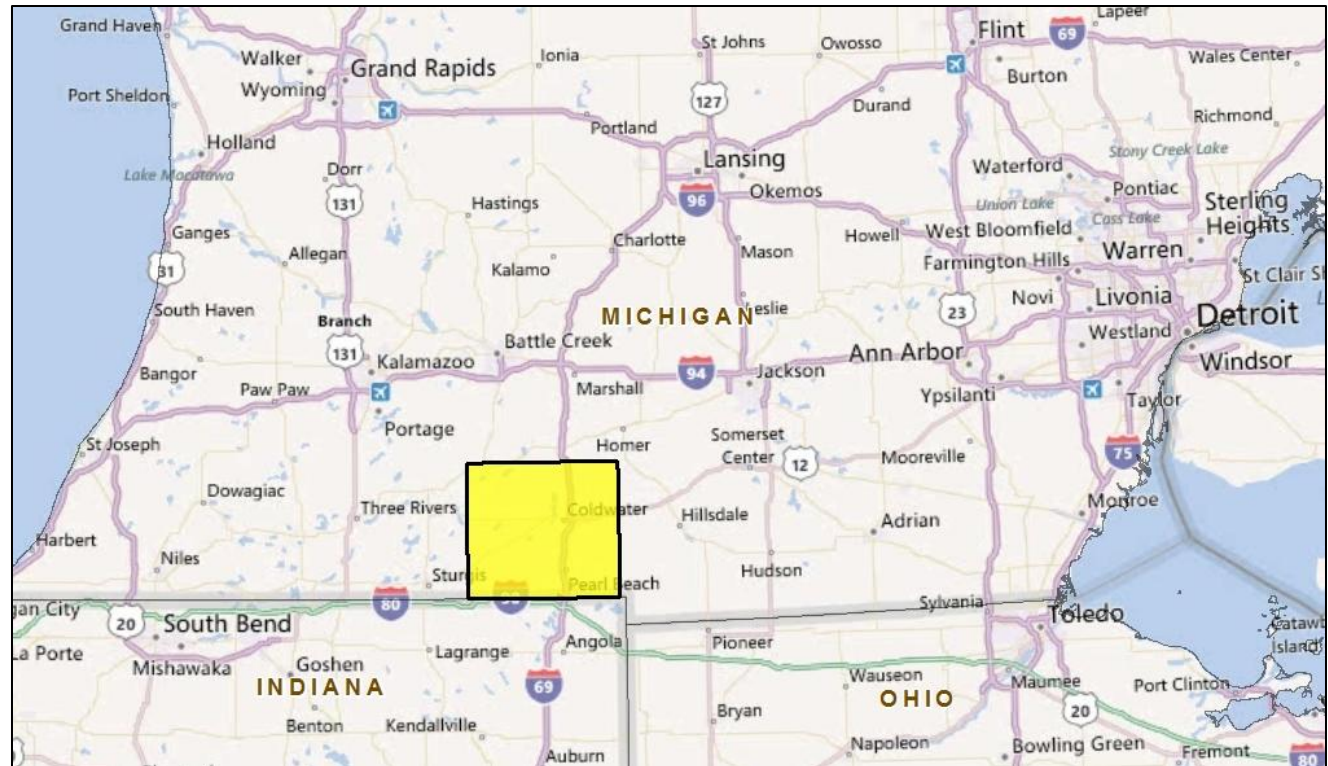
Sensitivity Analysis

Conclusion

Study Area

Branch County, Michigan

- Mainly Ag (65%)
- Well draining soils (85% B soils, 10% A)
- CLU data available



Regression-based Sensitivity

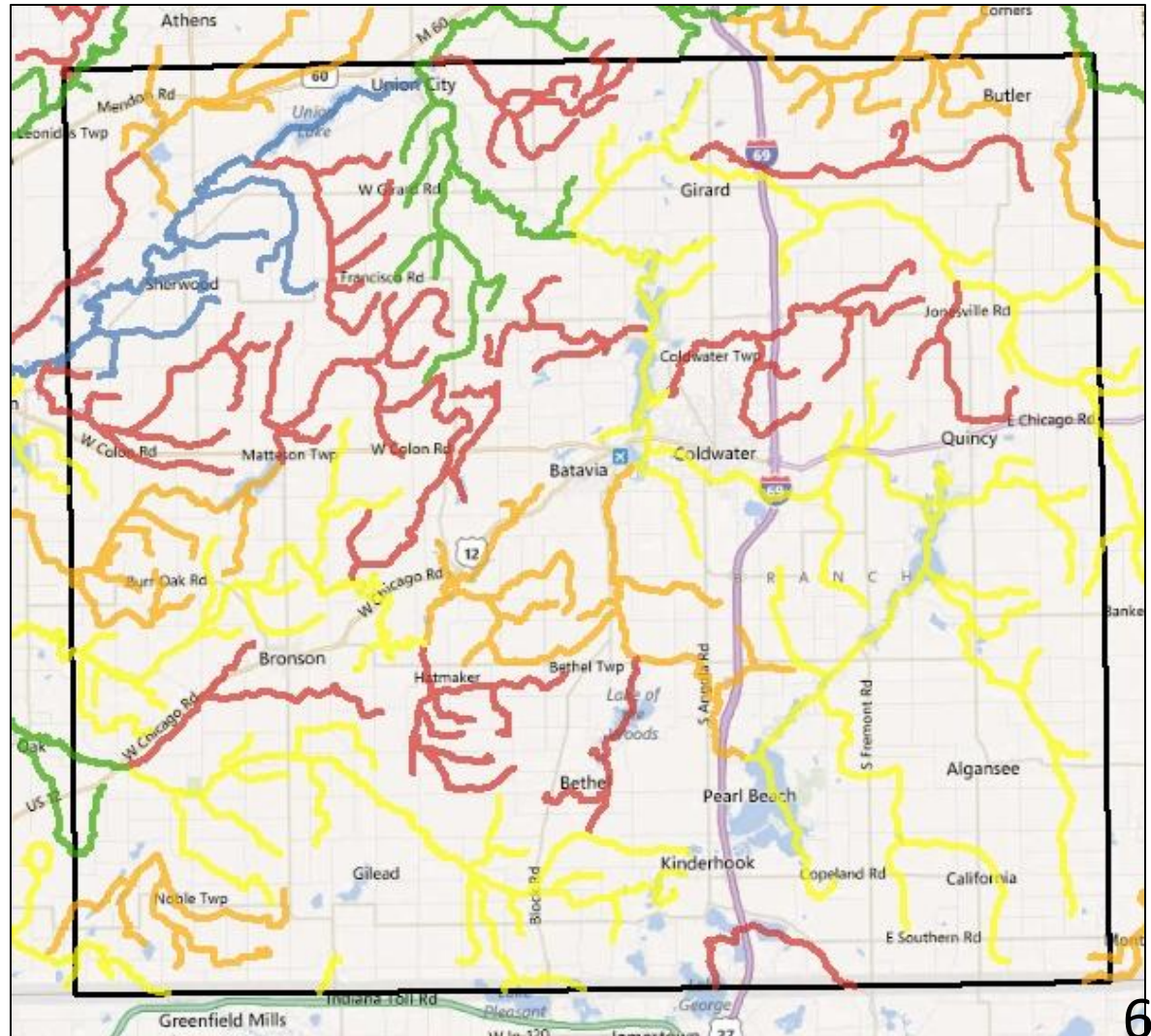
Fish Habitat Data

M-DNR:

- Tolerable baseflow reductions

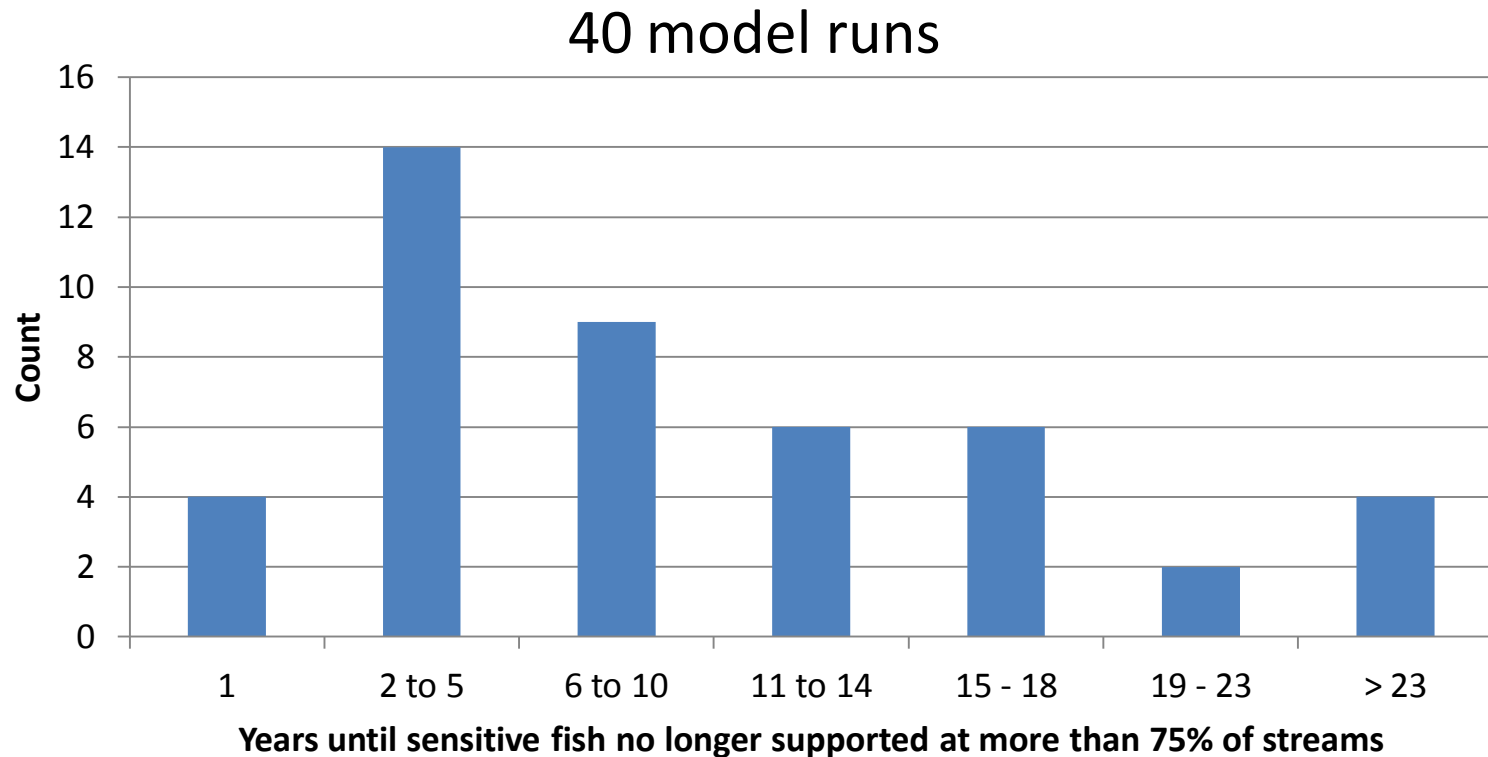
Sensitive Fish Sustainability Available GW Depletion (GPM)

- 107 - 243
- 244 - 515
- 516 - 1,887
- 1,888 - 3,140
- 3,141 - 10,507



Model Output / Dependent Variable

- Change in fish habitat sustainability over time (*Years To Stop*)
 - Reduction in baseflow
 - Change in stream fish habitat classification



Model Parameter Categories / Regression Independent Vars.

- Crops
 - area %
 - prices
 - price variability
- CRP enrollment
 - starting enrollment
 - probability of re-enrollment
 - contract length
- Land cover change probabilities
 - Given revenues of \$X, probability that a producer would convert Y to Z.
- Decision thresholds
 - revenue level above which producers will consider increased irrigation, below which they will consider CRP

Model Sensitivity Analysis

- Ran the model over 1,400 times with randomly selected parameter values
- Employed OLS regression
 - DV: Years until 75% of streams no longer support sensitive fish
 - IVs: model parameters

- Expectations

Starting corn prices	-	Revenue threshold to move land into production	+
Starting soy prices	-	Revenue threshold to move land into conservation	-
Corn area %	-	Ratio of market increase to CRP decrease	-
Soy area %	-	Starting % enrolled in CRP	+
Crop price variability	?	CRP contract length	+
Soy price variability	?	CRP renewal probability	+
Corn yield per acre	-	Probability of conversion to pasture	+
Soy yield per acre	-	Probability of conversion to forest	+
		Probability of conversion to wetland	+

Model Sensitivity Analysis

- Identified best models through an exhaustive approach
 - 17 model parameters
 - max of 7 independent variables at a time
 - 41,226 regressions
 - sorted by R², F-statistic, % of significant terms
- Is this rummaging?
 - Not trying to explore or discover variable relationships
 - The model is programmed to have relationships
 - Trying to identify weights of individual variables

Model Sensitivity Analysis

- Best OLS model

$$\ln(\text{Years to stop}) = 2.23 - (0.173 * \text{corn price}) - (0.141 * \text{corn price variability}) \\ - (0.009 * \text{corn yield}) - (0.010 * \text{soy yield}) \\ + (0.002 * \text{land production revenue threshold})$$

R2 0.35

F-statistic prob. < 0.001

Sig. ind. vars all

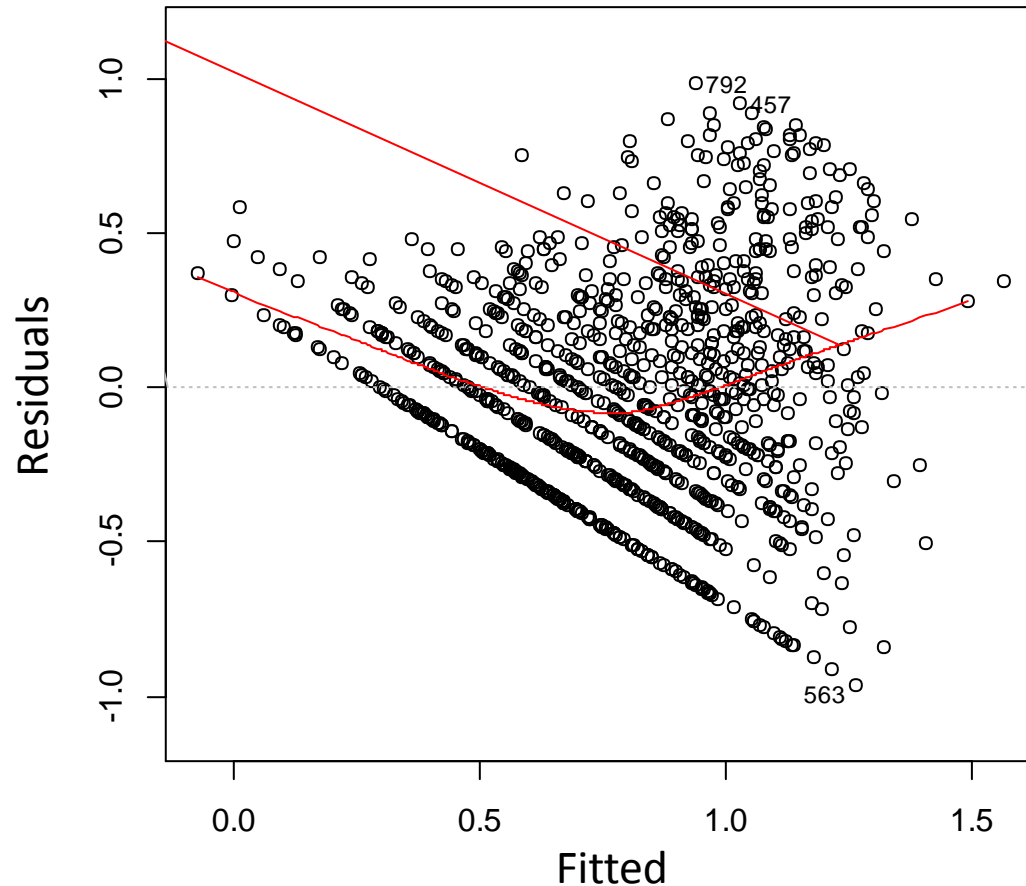
- Standardized coefficients

Corn price	-0.444
Soy yield	-0.328
Corn yield	-0.303
Land production revenue threshold	0.268
Corn price variability	-0.230

Model Sensitivity Analysis

Further inspection showed a poor fit

Residuals vs. Fitted Values



Why?

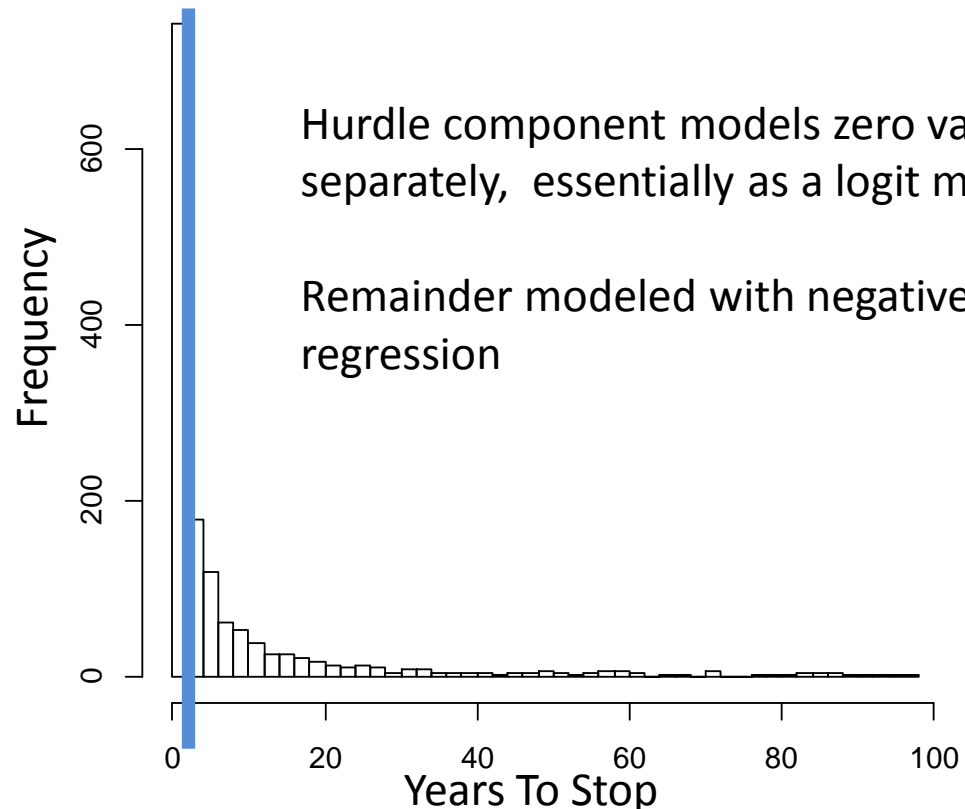
**DV is a count,
OLS won't work**

Model Sensitivity Analysis

- Employed a negative binomial regression, with a hurdle component as an alternative^{3,4}.

- Useful for over-dispersed, skewed data with large zero counts.

- Function *hurdle()* from the *pscl* R package.



3. cran.r-project.org/web/packages/pscl/vignettes/countreg.pdf

4. <http://www.ats.ucla.edu/stat/mplus/dae/nbreg.htm>

Model Sensitivity Analysis

- Best negative binomial hurdle model (sorted by AIC)

$$\begin{aligned}
 \text{Years to stop} = & 7.72 - (0.731 * \text{corn price}) - (0.657 * \text{corn price variability}) \\
 \text{(count model)} & - (0.038 * \text{corn yield}) - (0.047 * \text{soy yield}) \\
 & + (0.009 * \text{land production revenue threshold}) - \ln(\theta)
 \end{aligned}$$

$$\begin{aligned}
 \text{Years to stop} = & 6.76 - (0.352 * \text{corn price}) - (0.019 * \text{corn yield}) - (0.020 * \text{soy} \\
 \text{(zero model)} & \text{yield}) - \ln(\theta)
 \end{aligned}$$

Sig. ind. Vars All but θ

AIC 74741

- Difficult to standardize coefficients

Model Sensitivity Analysis

- Hurdle coefficient standardization options
 - z-score ratios

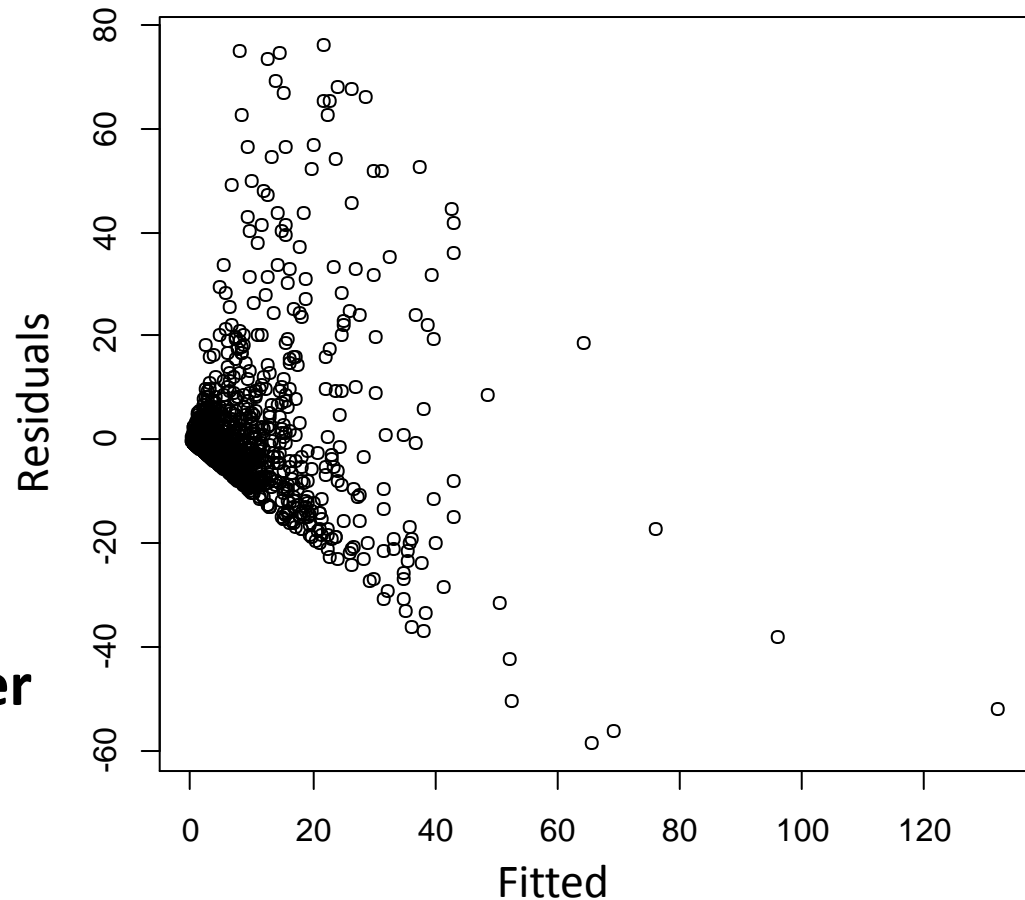
count model	Corn price	-0.349
	Soy yield	-0.298
	Corn yield	-0.260
	Corn price variability	-0.229
	Land production revenue threshold	0.137
zero model	Corn price	-0.386
	Soy yield	-0.309
	Corn yield	-0.305

- hierarchical partitioning
 - Murray and Connor 2009
 - R package *hier.part*

Model Sensitivity Analysis

Further inspection showed hurdle was still a poor fit

Residuals vs. Fitted Values



Why?

**Still struggling
with skewness.**

**Transformation of
DV makes it no longer
a count.**

- Regression can be utilized to estimate parameter weights in complex spatial model.
- Issues arise when the dependent variable is count data
 - Poisson and negative binomial regression are viable alternatives for over-dispersed data
 - hurdle models for large zero counts
- Dependent variable skewness is significant challenge
 - normally distributed continuous data is preferable
 - not always feasible for agent-based models based on steps
- The example fish habitat sustainability model was most sensitive to market-based parameters (corn price, price variability, production revenue thresholds).

Special Thanks:

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References:

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Murray, K., Connor, M. 2009. “Methods to Quantify Variable Importance: implications for the analysis of noisy ecological data.” *Ecology*, 90(2): p. 348-355.